

Probabilistic Topic Models and User Behavior

David M. Blei
Columbia University

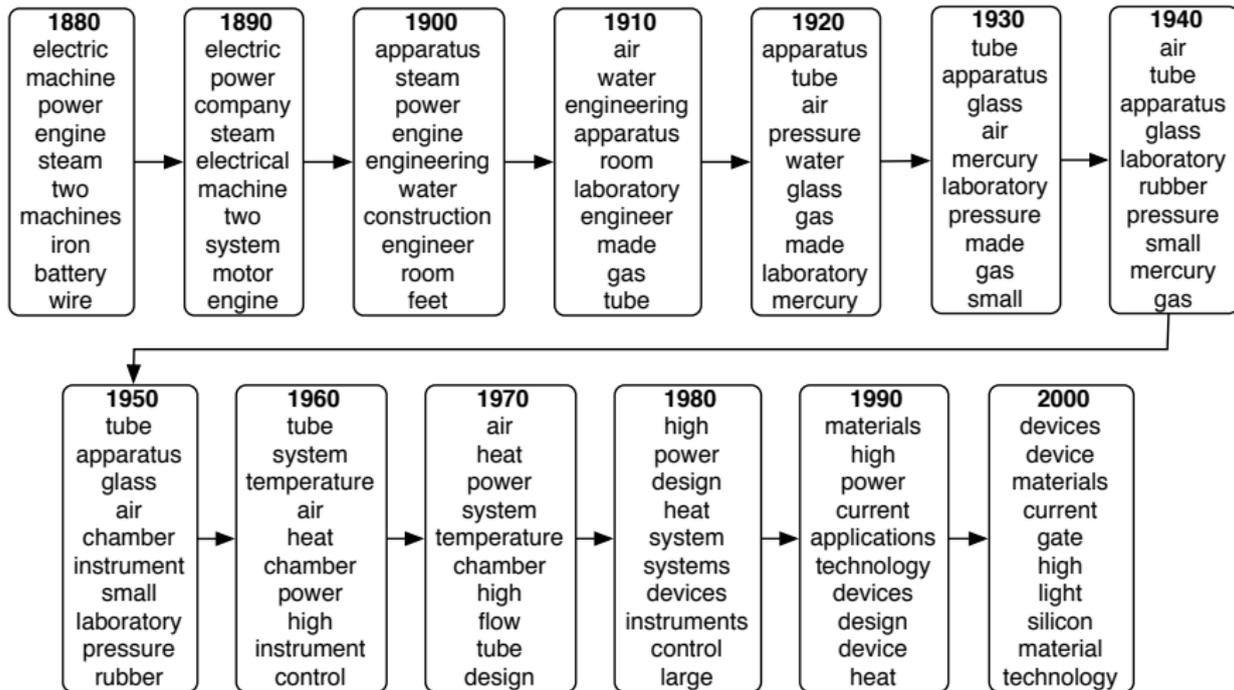


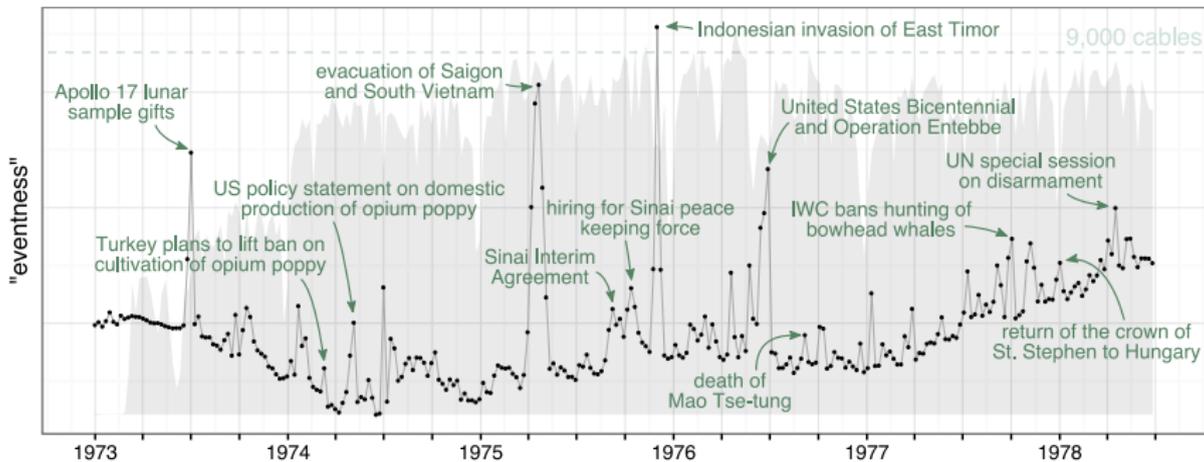
- ▶ **ORGANIZE**
- ▶ **VISUALIZE**
- ▶ **SUMMARIZE**
- ▶ **SEARCH**
- ▶ **PREDICT**
- ▶ **UNDERSTAND**



TOPIC MODELING

1. **Discover** the thematic structure
2. **Annotate** the documents
3. **Use** the annotations to visualize, organize, summarize, ...







SKY WATER TREE
MOUNTAIN PEOPLE



SCOTLAND WATER
FLOWER HILLS TREE



SKY WATER BUILDING
PEOPLE WATER



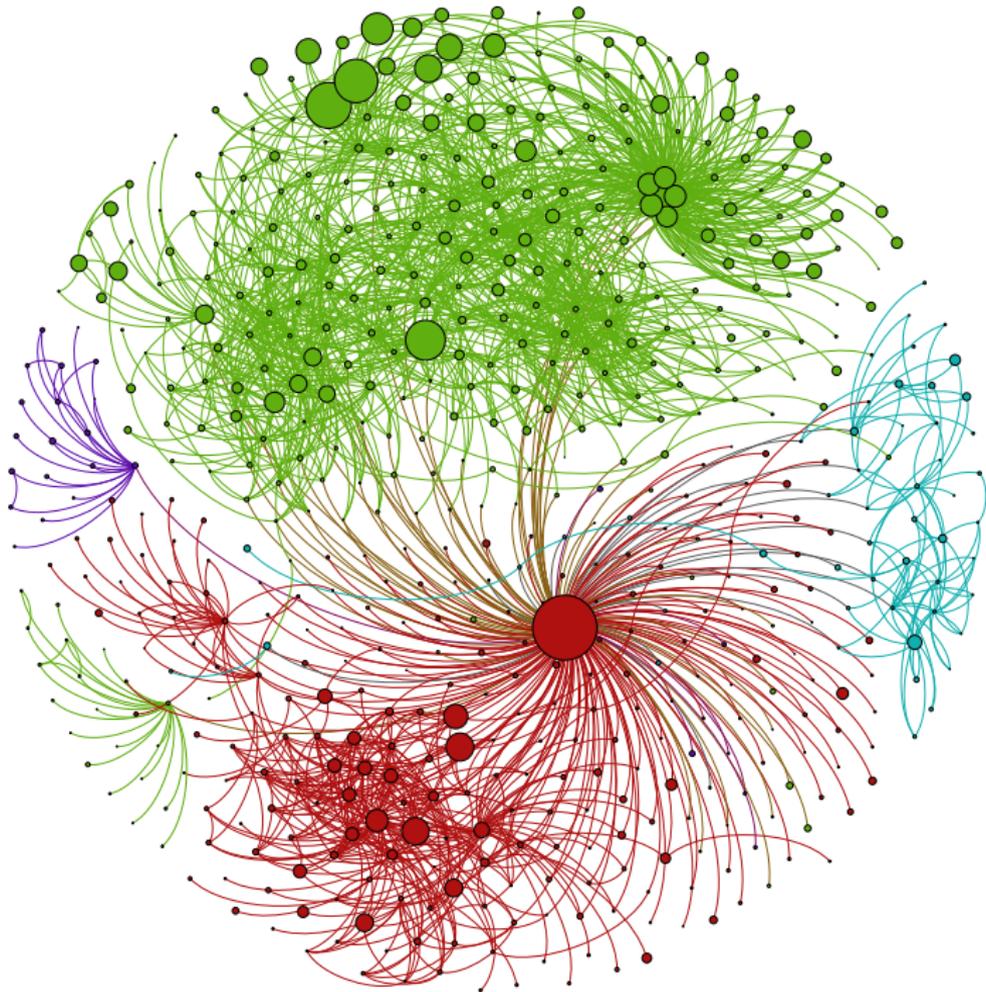
FISH WATER OCEAN
TREE CORAL

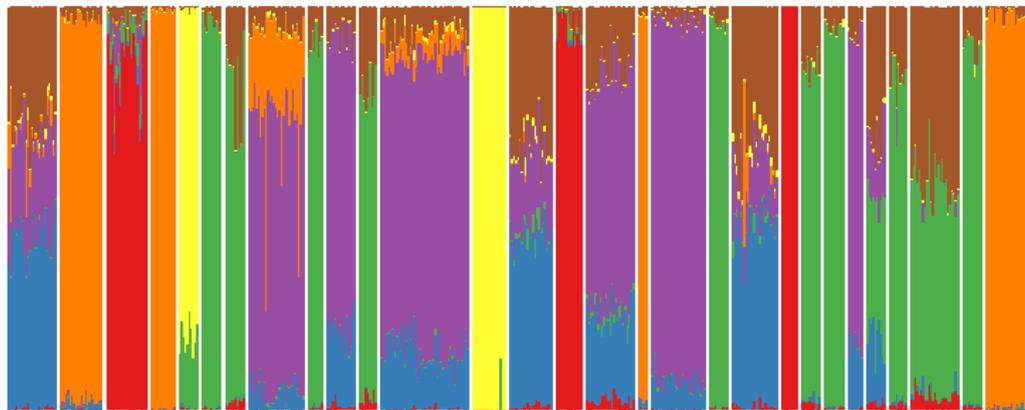
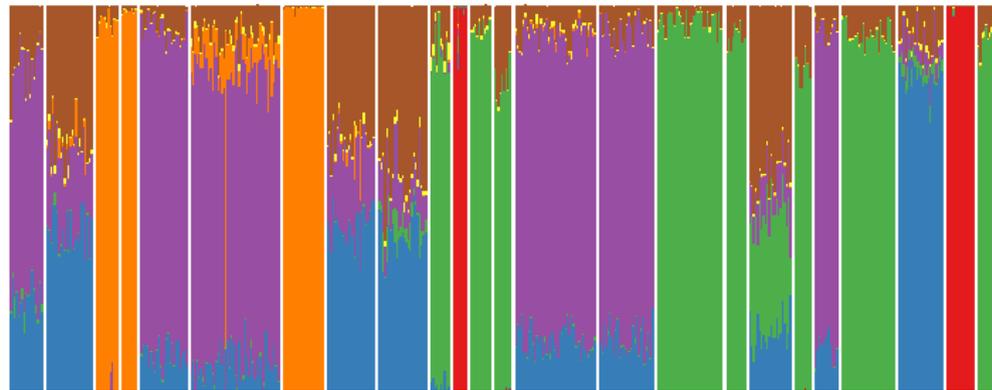


PEOPLE MARKET PATTERN
TEXTILE DISPLAY



BIRDS NEST TREE
BRANCH LEAVES







Charles Darwin's library



The NYC subway

- ▶ **People read documents.**
- ▶ These might be people for whom we want to form predictions.
- ▶ And, their behavior is an additional signal about the meaning of the documents and the organization of the collection.

This talk

1. Introduction to topic modeling
2. Recommendation and exploration with collaborative topic models
3. The bigger picture: Using probability models to solve problems with data

Introduction to Topic Modeling

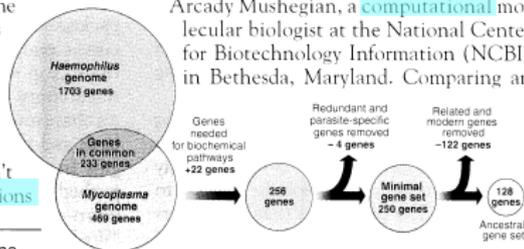
Seeking Life's Bare (Genetic) Necessities

COLD SPRING HARBOR, NEW YORK—How many genes does an organism need to survive? Last week at the genome meeting here,* two genome researchers with radically different approaches presented complementary views of the basic genes needed for life. One research team, using computer analyses to compare known genomes, concluded that today's organisms can be sustained with just 250 genes, and that the earliest life forms required a mere 128 genes. The other researcher mapped genes in a simple parasite and estimated that for this organism, 800 genes are plenty to do the job—but that anything short of 100 wouldn't be enough.

Although the numbers don't match precisely, those predictions

“are not all that far apart,” especially in comparison to the 75,000 genes in the human genome, notes Siv Andersson of Uppsala University in Sweden, who arrived at the 800 number. But coming up with a consensus answer may be more than just a genetic numbers game, particularly as more and more genomes are completely mapped and sequenced. “It may be a way of organizing any newly sequenced genome,” explains

Arcady Mushegian, a computational molecular biologist at the National Center for Biotechnology Information (NCBI) in Bethesda, Maryland. Comparing an



Stripping down. Computer analysis yields an estimate of the minimum modern and ancient genomes.

* Genome Mapping and Sequencing, Cold Spring Harbor, New York, May 8 to 12.

Documents exhibit multiple topics.

Topics

gene 0.04
dna 0.02
genetic 0.01
...

life 0.02
evolve 0.01
organism 0.01
...

brain 0.04
neuron 0.02
nerve 0.01
...

data 0.02
number 0.02
computer 0.01
...

Documents

Seeking Life's Bare (Genetic) Necessities

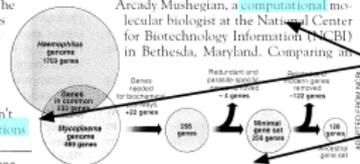
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SCIENCE • VOL. 272 • 24 MAY 1996

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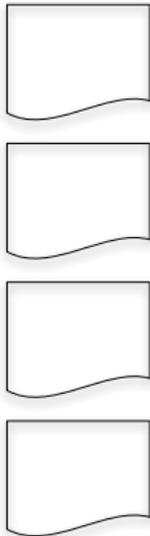
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Topic proportions and assignments



Latent Dirichlet Allocation

Topics



Documents

Topic proportions and assignments

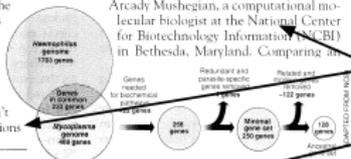
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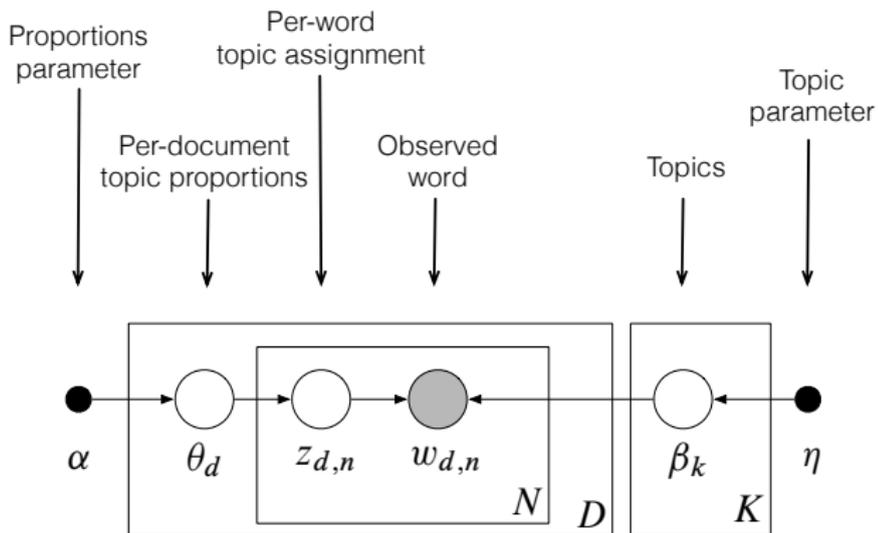
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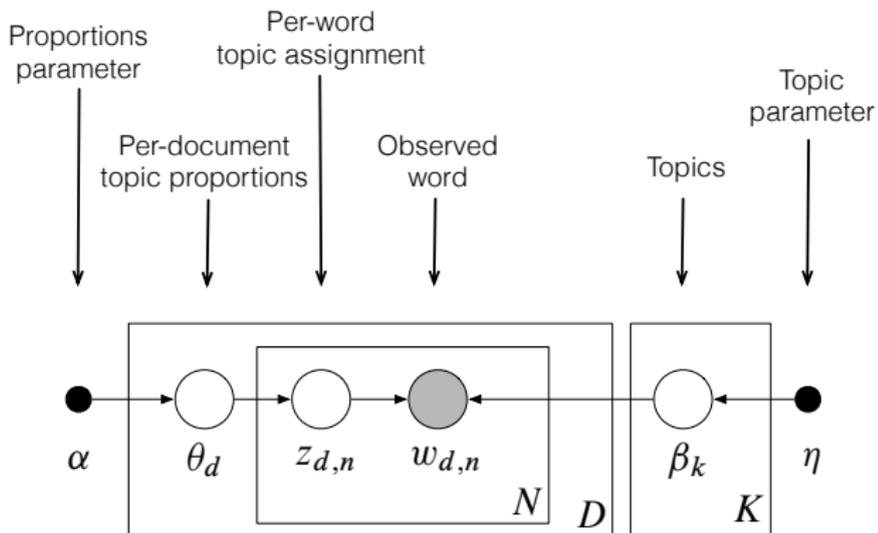
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Latent Dirichlet Allocation



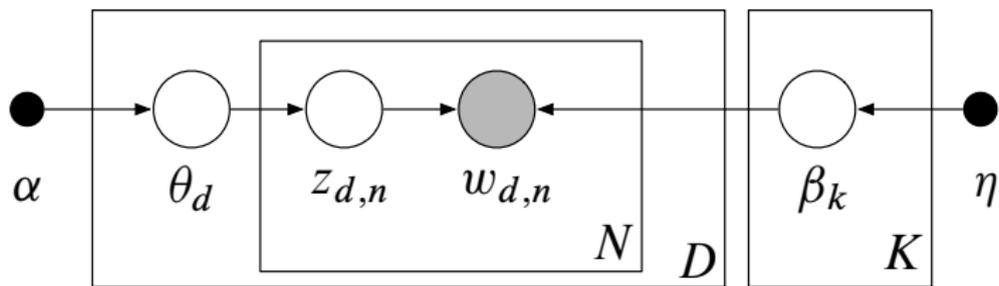
LDA as a graphical model

- ▶ Nodes are random variables; edges indicate dependence.
- ▶ Shaded nodes are observed; unshaded nodes are hidden.
- ▶ Plates indicate replicated variables.

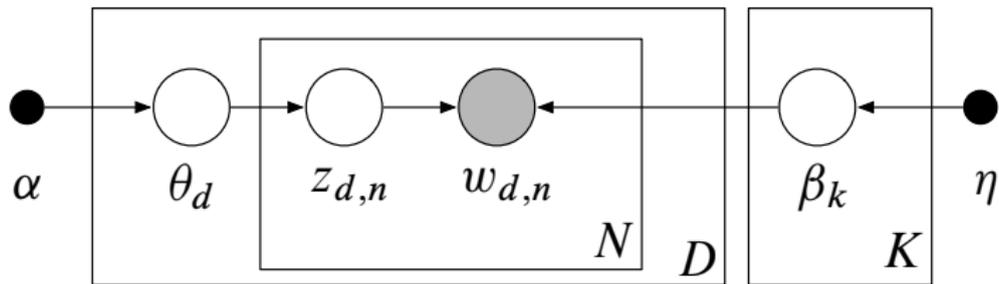


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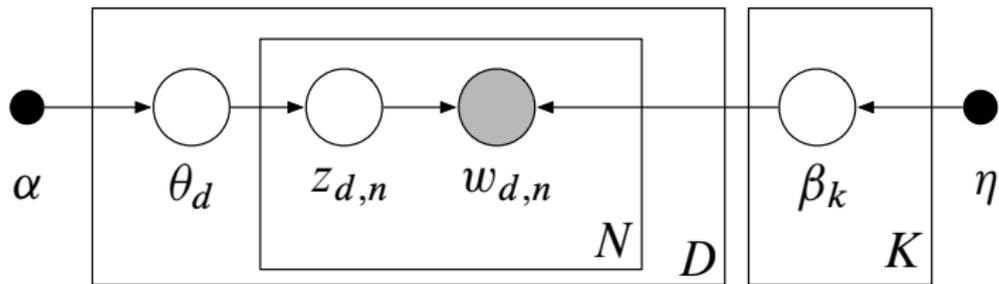
- ▶ Defines a factorization of the joint probability distribution
- ▶ Encodes independence assumptions about the variables
- ▶ Connects to algorithms for computing with data



- ▶ The joint defines a posterior, $p(\theta, z, \beta | w)$.
- ▶ From a collection of documents, infer
 - Per-word topic assignment $z_{d,n}$
 - Per-document topic proportions θ_d
 - Per-corpus topic distributions β_k
- ▶ Then use posterior expectations to perform the task at hand: information retrieval, document similarity, exploration, and others.



- ▶ Mean field variational methods (Blei et al., 2001, 2003)
- ▶ Expectation propagation (Minka and Lafferty, 2002)
- ▶ Collapsed Gibbs sampling (Griffiths and Steyvers, 2002)
- ▶ Distributed sampling (Newman et al., 2008; Ahmed et al., 2012)
- ▶ Collapsed variational inference (Teh et al., 2006)
- ▶ Stochastic inference (Hoffman et al., 2010, 2013; Mimno et al., 2012)
- ▶ Factorization inference (Arora et al., 2012; Anandkumar et al., 2012)
- ▶ Amortized inference (Srivastava and Sutton, 2016)



- ▶ LDA in R [<https://cran.r-project.org/web/packages/lda/>]
- ▶ GenSim [<https://radimrehurek.com/gensim/>]
- ▶ Mallet [<http://mallet.cs.umass.edu>]
- ▶ Vowpal Wabbit [<http://hunch.net/~vw/>]
- ▶ Apache Spark [<http://spark.apache.org/>]
- ▶ SciKit Learn [<http://scikit-learn.org/>]

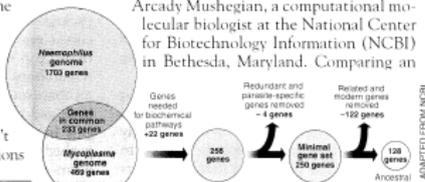


- ▶ **Data:** The OCR'ed collection of *Science* from 1990–2000
 - 17K documents
 - 11M words
 - 20K unique terms (stop words and rare words removed)
- ▶ **Model:** 100-topic LDA model using variational inference.

Seeking Life's Bare (Genetic) Necessities

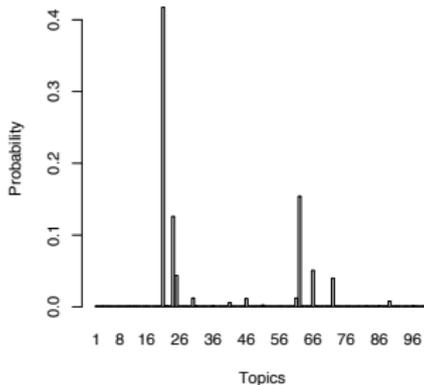
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human	evolution	disease	computer
genome	evolutionary	host	models
dna	species	bacteria	information
genetic	organisms	diseases	data
genes	life	resistance	computers
sequence	origin	bacterial	system
gene	biology	new	network
molecular	groups	strains	systems
sequencing	phylogenetic	control	model
map	living	infectious	parallel
information	diversity	malaria	methods
genetics	group	parasite	networks
mapping	new	parasites	software
project	two	united	new
sequences	common	tuberculosis	simulations

1

Game
Season
Team
Coach
Play
Points
Games
Giants
Second
Players

2

Life
Know
School
Street
Man
Family
Says
House
Children
Night

3

Film
Movie
Show
Life
Television
Films
Director
Man
Story
Says

4

Book
Life
Books
Novel
Story
Man
Author
House
War
Children

5

Wine
Street
Hotel
House
Room
Night
Place
Restaurant
Park
Garden

6

Bush
Campaign
Clinton
Republican
House
Party
Democratic
Political
Democrats
Senator

7

Building
Street
Square
Housing
House
Buildings
Development
Space
Percent
Real

8

Won
Team
Second
Race
Round
Cup
Open
Game
Play
Win

9

Yankees
Game
Mets
Season
Run
League
Baseball
Team
Games
Hit

10

Government
War
Military
Officials
Iraq
Forces
Iraqi
Army
Troops
Soldiers

11

Children
School
Women
Family
Parents
Child
Life
Says
Help
Mother

12

Stock
Percent
Companies
Fund
Market
Bank
Investors
Funds
Financial
Business

13

Church
War
Women
Life
Black
Political
Catholic
Government
Jewish
Pope

14

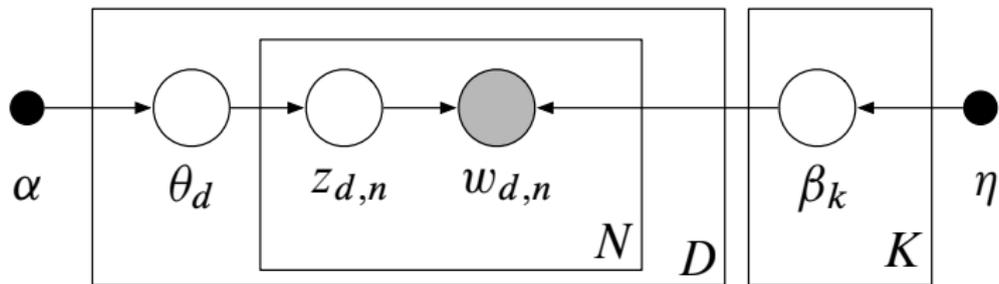
Art
Museum
Show
Gallery
Works
Artists
Street
Artist
Paintings
Exhibition

15

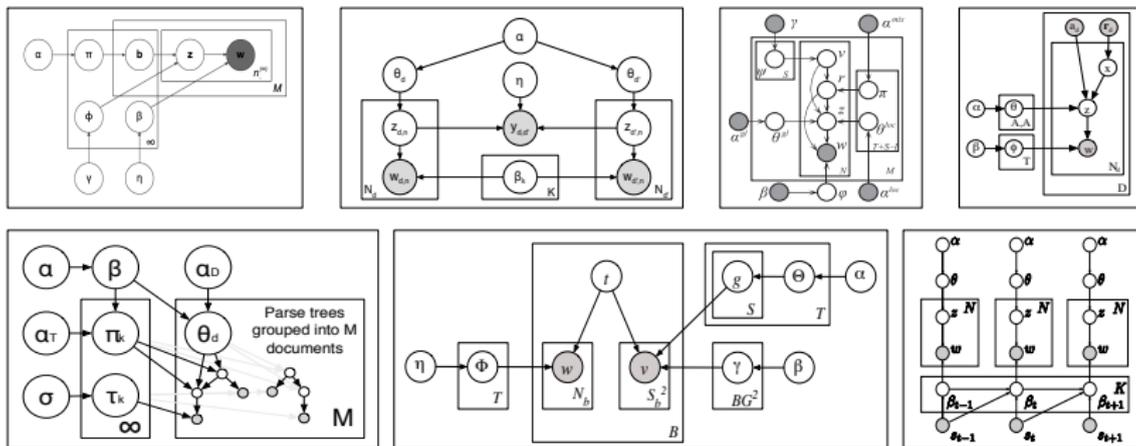
Police
Yesterday
Man
Officer
Officers
Case
Found
Charged
Street
Shot

How does LDA “work”?

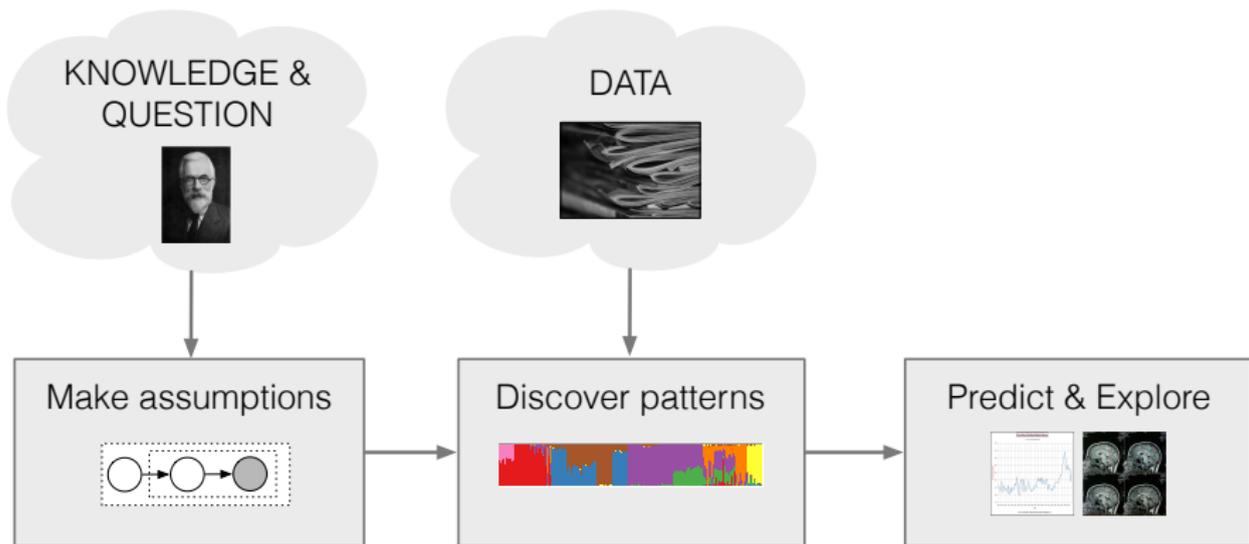
- ▶ LDA trades off two goals.
 1. In each **document**, allocate its words to **few topics**.
 2. In each **topic**, assign high probability to **few terms**.
- ▶ These goals are at odds.
 - Putting a document in a single topic makes #2 hard:
All of its words must have probability under that topic.
 - Putting very few words in each topic makes #1 hard:
To cover a document’s words, it must assign many topics to it.
- ▶ Trading off these goals finds groups of tightly co-occurring words.



- ▶ Summary: LDA discovers themes through posterior inference.
- ▶ Other perspectives
 - Latent semantic analysis [Deerwester et al., 1990; Hofmann, 1999]
 - A mixed-membership model [Erosheva, 2004]
 - PCA and matrix factorization [Jakulin and Buntine, 2002]
 - Was independently invented for genetics [Pritchard et al., 2000]



- ▶ LDA has become a building block that enables many applications.
- ▶ Algorithmic improvements let us fit models to massive data.
(See VW, Gensim, Mallet, others.)
- ▶ Organizing and finding patterns in text is important in the sciences, humanities, industry, and culture.



- ▶ Case study in **text analysis with probability models**
- ▶ Topic modeling research
 - develops new models.
 - develops new inference algorithms.
 - develops new applications, visualizations, tools.

Collaborative Topic Models

with Prem Gopalan, Laurent Charlin, and Chong Wang



Charles Darwin's library

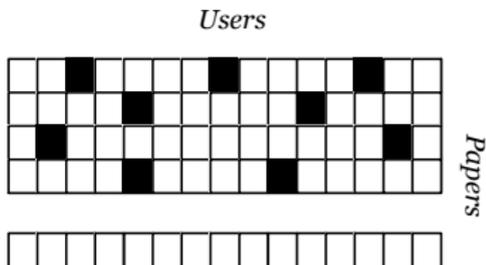


Reading on the New York subway

- ▶ **People read documents.**
- ▶ *Collaborative topic models* connect content to consumption

Maximum likelihood from incomplete data via the EM algorithm
Conditional Random Fields
Introduction to Variational Methods for Graphical Models
The Mathematics of Statistical Machine Translation

Topic Models for Recommendation



- ▶ Example: Scientists share their research libraries.
- ▶ Collaborative topic models can
 - Helps readers discover documents, old and new.
 - Describe readers in terms of topical preferences
 - Identify documents that are impactful, interdisciplinary

- ▶ Consider EM (Dempster et al., 1977). We infer topics from its text:

Maximum Likelihood from Incomplete Data via the EM Algorithm

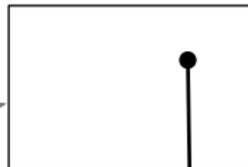
By A. P. DEMPSTER, N. M. LAIRD and D. B. RUBIN

Harvard University and Educational Testing Service

[Read before the ROYAL STATISTICAL SOCIETY at a meeting organized by the RESEARCH SECTION on Wednesday, December 8th, 1976, Professor S. D. SILVEY in the Chair]

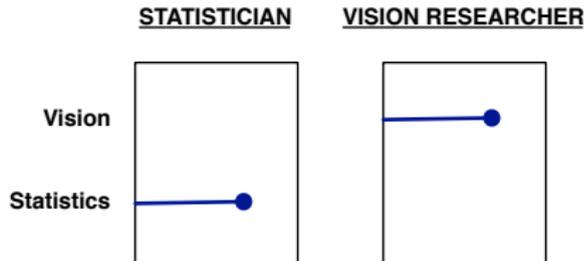
SUMMARY

A broadly applicable algorithm for computing maximum likelihood estimates from incomplete data is presented at various levels of generality. Theory showing the monotone behaviour of the likelihood and convergence of the algorithm is derived. Many examples are sketched, including missing value situations, applications to grouped, censored or truncated data, finite mixture models, variance component estimation, hyperparameter estimation, iteratively reweighted least squares and factor analysis.



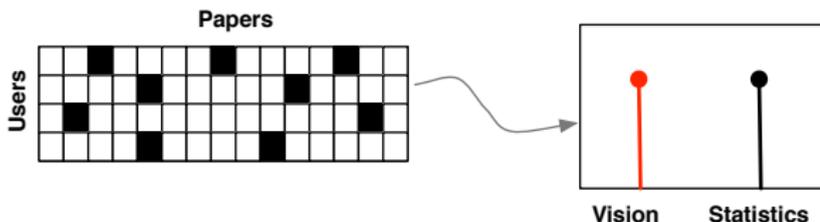
Vision Statistics

- ▶ Suppose there are two types of scientists

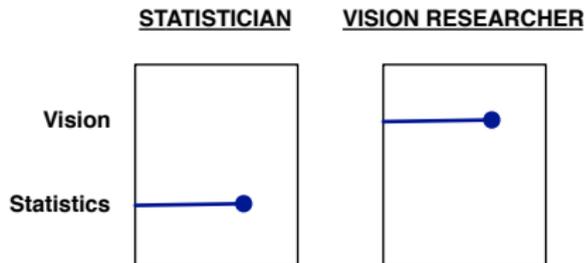


- ▶ We first recommend the EM paper to **statisticians**.

- ▶ With user data, we can adjust the topics to account for who liked it:



- ▶ Consider again the scientists



- ▶ We now recommend the EM paper to **vision researchers**.

Maximum Likelihood from Incomplete Data via the *EM* Algorithm

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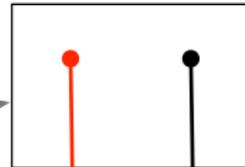
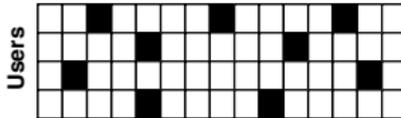
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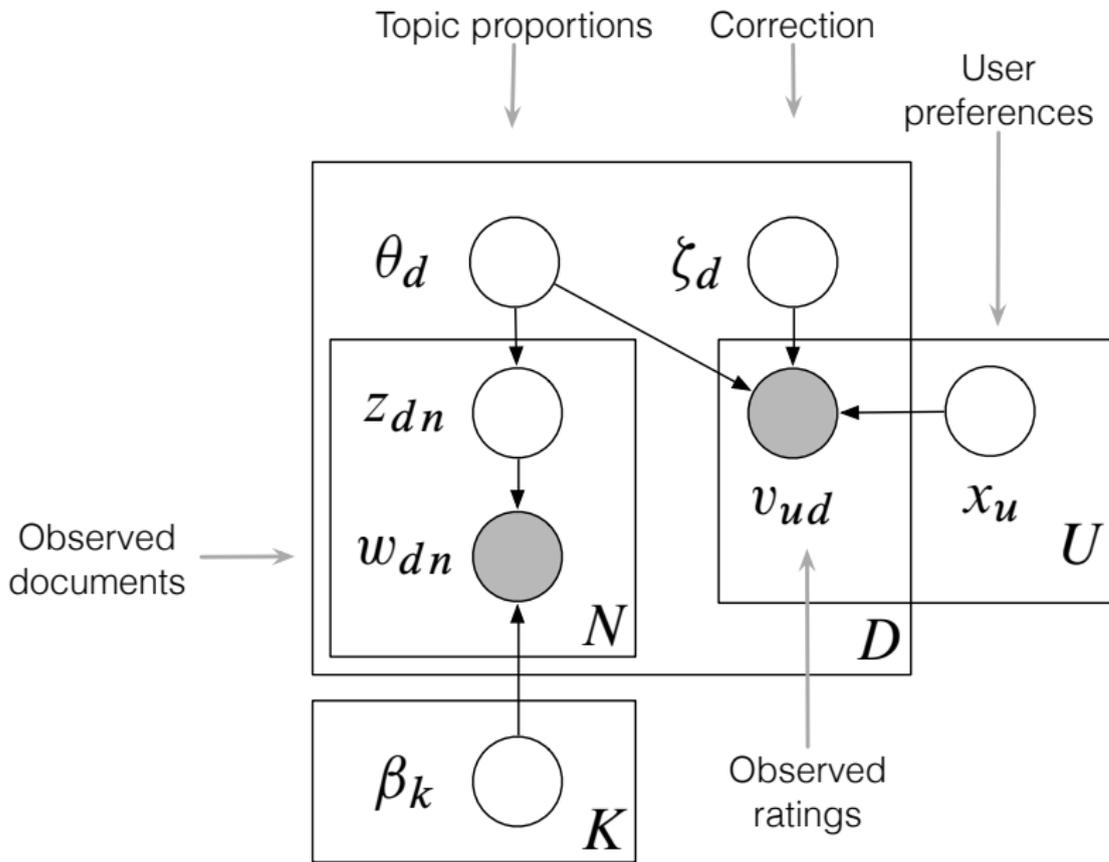
Papers

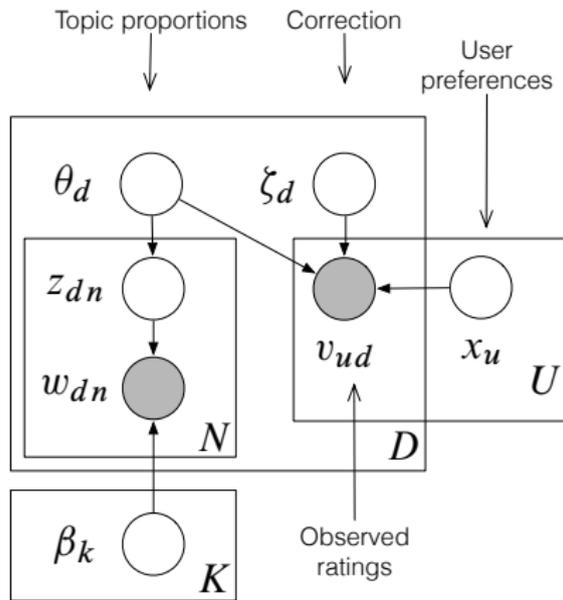


Vision Statistics

Without text, we cannot initially recommend to anyone.

Without user data, we cannot recommend to vision researchers.





$$\begin{aligned} \theta_{dk} &\sim \text{Gamma}(\cdot, \cdot) \\ \zeta_{dk} &\sim \text{Gamma}(\cdot, \cdot) \\ x_{uk} &\sim \text{Gamma}(\cdot, \cdot) \\ v_{ud} &\sim \text{Poisson}((\theta_d + \zeta_d)^\top x_u) \end{aligned}$$

- ▶ Blends factorization-based and content-based recommendation
- ▶ Describes user preferences with interpretable topics
- ▶ Builds on Poisson factorization

[Canney 2004; Dunson and Herring 2005; Gopalan et al. 2014]



- ▶ Big data set from Mendeley.com
- ▶ The data:
 - 261K documents
 - 80K users
 - 10K vocabulary terms
 - 25M observed words
 - 5.1M entries (sparsity is 0.02%)

Maximum Likelihood from Incomplete Data via the *EM* Algorithm

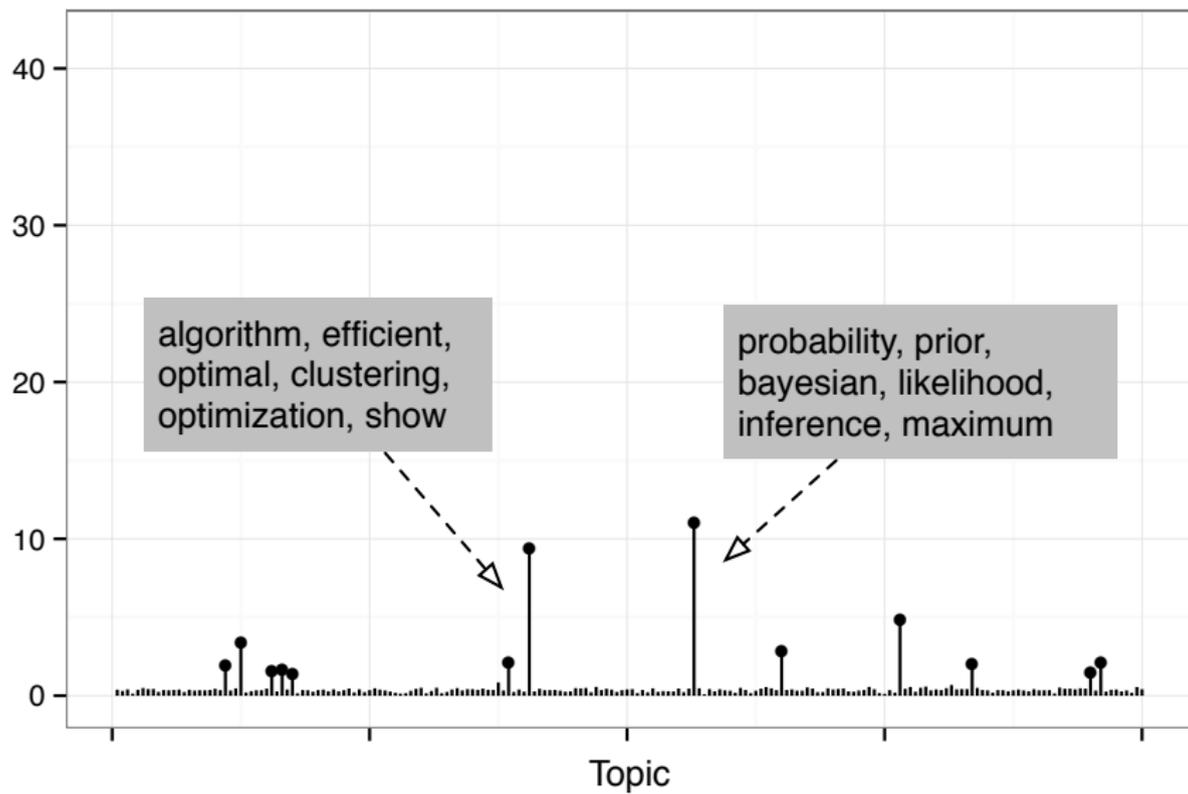
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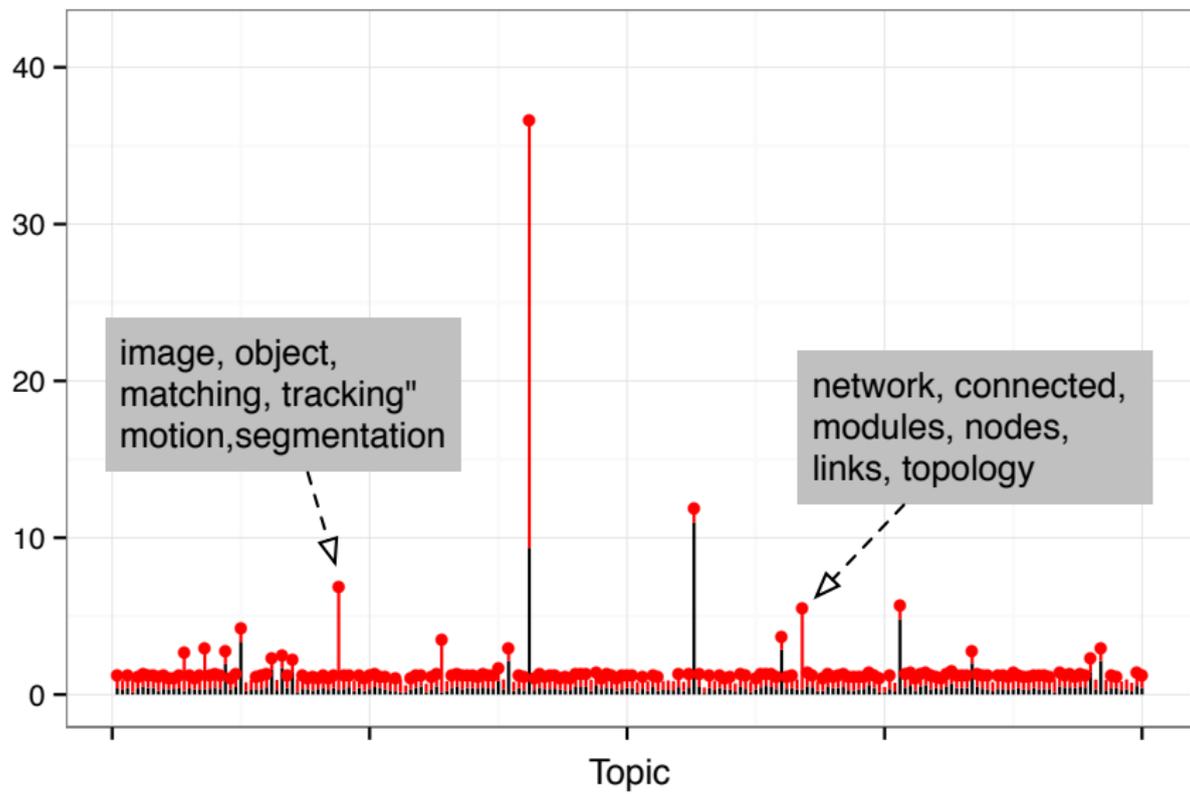
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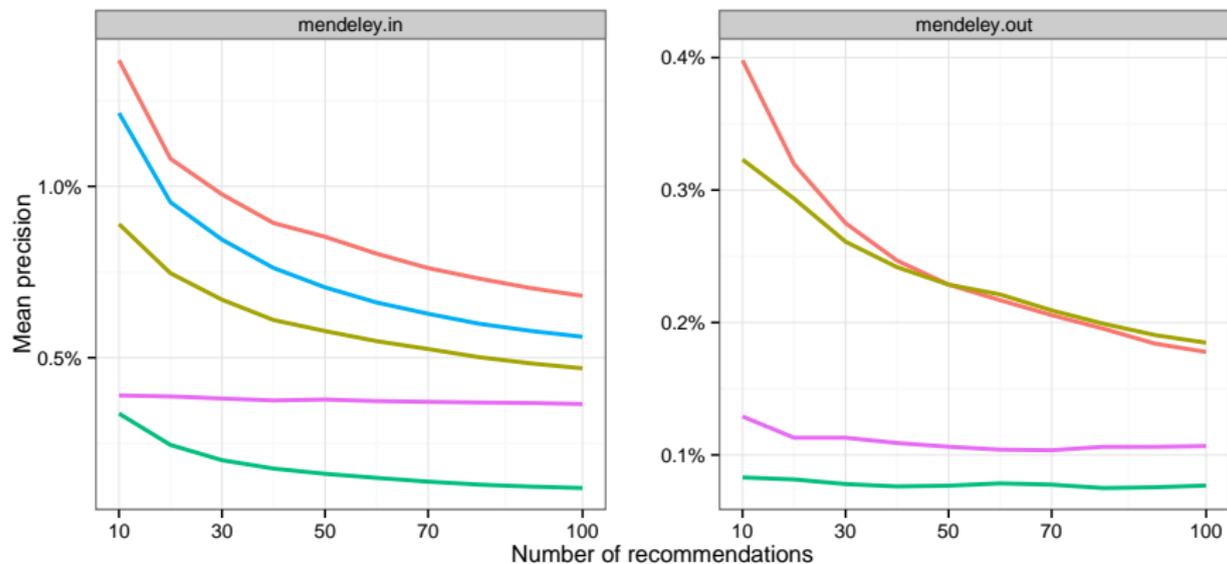
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Mendeley

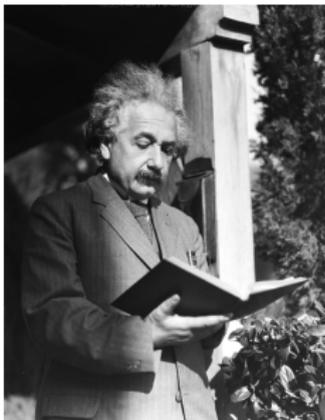


Method

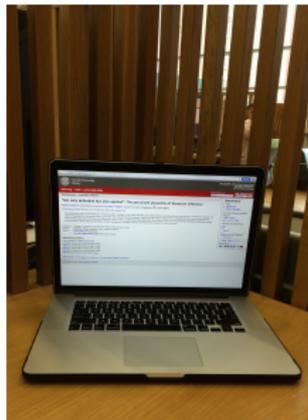
- Collaborative Poisson Topic Factorization
- Decoupled Poisson Factorization
- Content Only
- Ratings Only (Gopalan et al., 2014)
- Collaborative Topic Regression (Wang and Blei, 2011)



Darwin's library



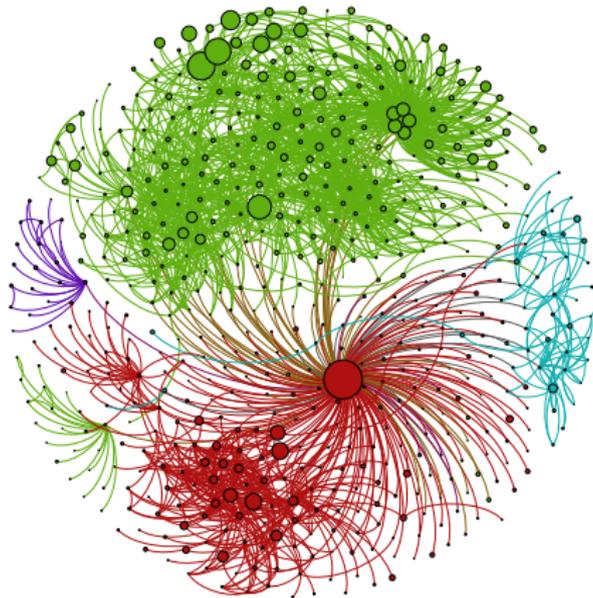
Einstein reading



Another scientist reading

- ▶ The readers also **tell us about the articles.**
- ▶ We can look at posterior estimates to find
 - Interdisciplinary articles
 - Influential articles within a field
 - Outside influences on a field

“Network Analysis”



network; connected; modules; nodes; links; topology; connectivity; graph;
robustness; connections; modular; world; degree; properties

Assortative mixing in networks

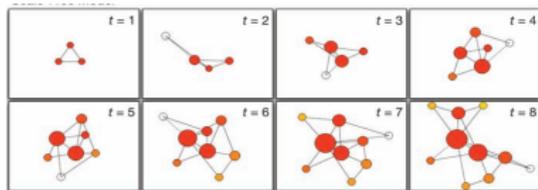
M. E. J. Newman

*Department of Physics, University of Michigan, Ann Arbor, MI 48109-1120 and
Santa Fe Institute, 1399 Hyde Park Road, Santa Fe, NM 87501*



About networks

- ▶ Assortative mixing in networks
(Newman, 2002)
- ▶ Mixing patterns in networks
(Newman, 2002)
- ▶ Catastrophic cascade of failures in interdependent networks
(Buldyrev et al., 2010)



About networks; for readers of networks

- ▶ Emergence of scaling in random networks
(Barabassi and Albert, 1999)
- ▶ Statistical mechanics of complex networks
(Albert and Barabassi, 2002)
- ▶ Complex networks: Structure and dynamics
(Boccaletti et al., 2006)

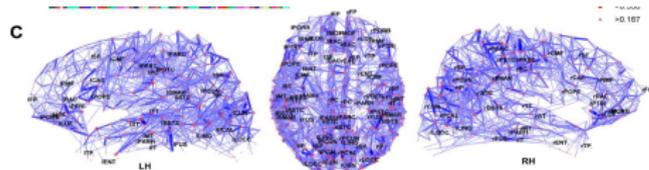
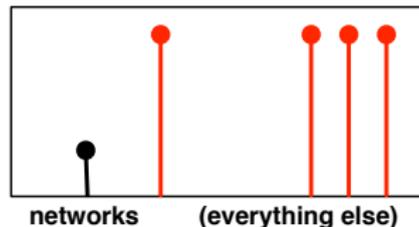
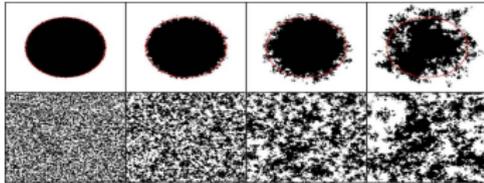


Figure 3. High-Resolution Connection Matrix, Network Layout and Connectivity Backbone (Participant A, scan 2)



About networks; for readers of other fields

- ▶ Mapping the Structural Core of Human Cerebral Cortex
(Hagmann et al., 2008)
- ▶ Network thinking in ecology and evolution
(Proulx et al., 2005)
- ▶ Linked: The New Science of Networks
(Barabasi, 2002)



networks (everything else)

Not about networks; for readers of networks

- ▶ Power-law distributions in empirical data
(Clauset et al., 2009)
- ▶ Statistical physics of social dynamics
(Castellano et al., 2009)
- ▶ The origin of bursts and heavy tails in human dynamics
(Barabasi, 2005)

“Statistical Modeling”

About this field; read by users in this field

- ▶ A Bayesian analysis of some nonparametric problems
- ▶ Bayesian measures of model complexity and fit
- ▶ Monte Carlo Methods in Bayesian Computation

About this field; read by users in other fields

- ▶ A tutorial on HMMs and selected applications in speech recognition
- ▶ An Introduction to Bayesian Networks and Influence Diagrams
- ▶ Maximum likelihood from incomplete data via the EM algorithm

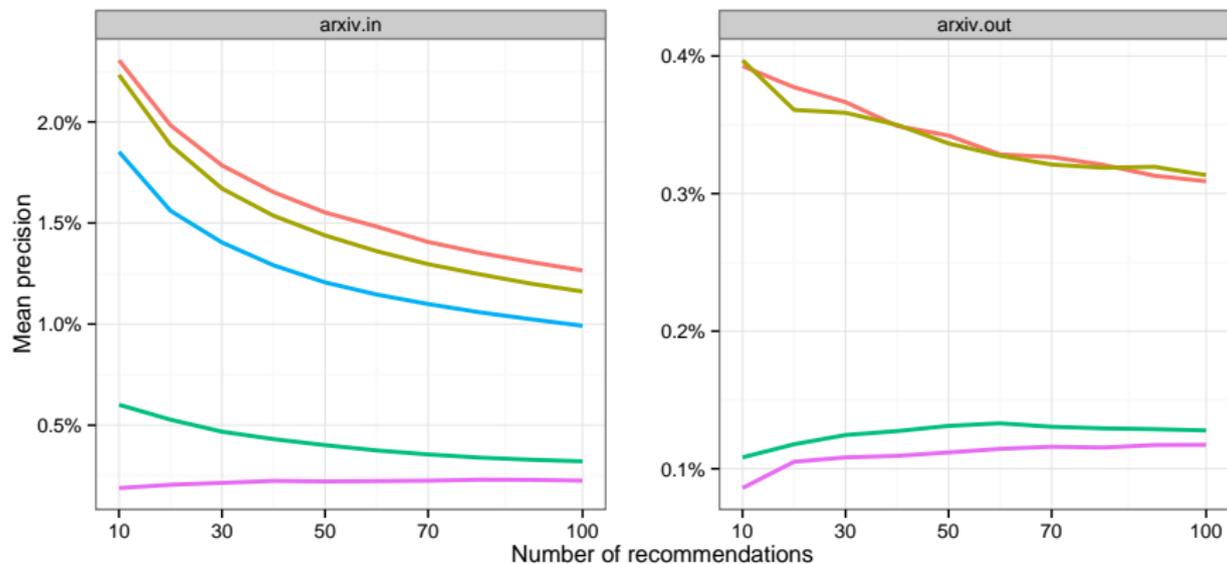
About other fields; read by users in this field

- ▶ Second Thoughts on the Bootstrap
- ▶ A guide to Eclipse and the R plug-in StatET
- ▶ Using Multivariate Statistics



- ▶ A decade of clicks on arXiv.org (2003–2013)
- ▶ The data:
 - 826K documents
 - 120K users
 - 14K vocabulary terms
 - 54M observed words
 - 43.6M entries (sparsity is 0.04%)

arXiv click history



Method

- Collaborative Poisson Topic Factorization
- Decoupled Poisson Factorization
- Content Only
- Ratings Only (Gopalan et al., 2014)
- Collaborative Topic Regression (Wang and Blei, 2011)

Stat.ML: Machine Learning

In stat.ML; for stat.ML readers

- ▶ Noisy matrix decomposition via convex relaxation
- ▶ Robust computation of linear models, or how to find a needle in a haystack
- ▶ High-dimensional regression with noisy and missing data

In stat.ML; for other readers

- ▶ Co-evolution of selection and influence in social networks
- ▶ Hierarchical structure and the prediction of missing links in networks
- ▶ Learning continuous-time social network dynamics

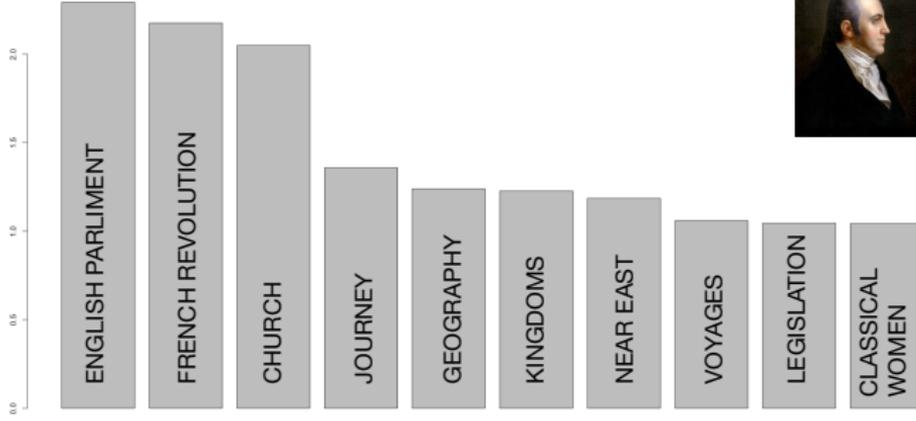
In other categories; for stat.ML readers

- ▶ Finding structure with randomness
- ▶ Representation learning: A review and new perspectives
- ▶ Computational and statistical tradeoffs via convex relaxation

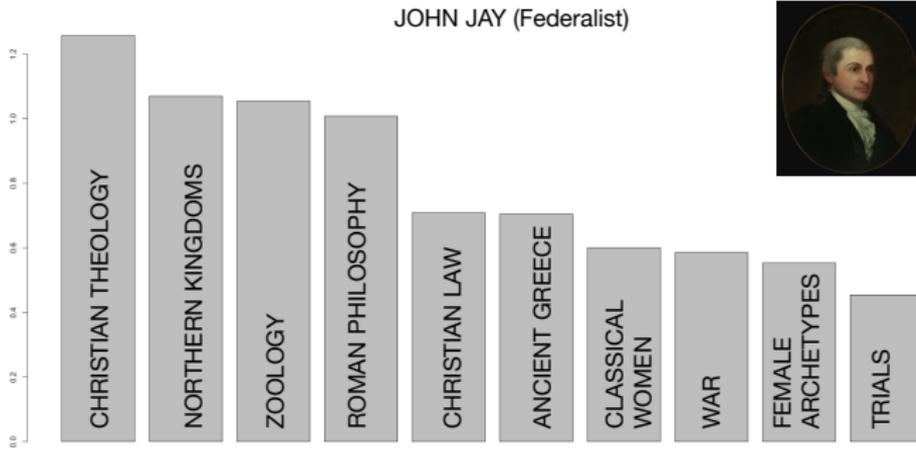


- ▶ The New York Society library is the first library in New York City (1754)
- ▶ Mark Hoffman and Peter Bearman (sociology) are using collaborative topic models to explore the usage patterns of important figures in U.S. History
- ▶ The data
 - 1789 – 1806
 - 847 users (people like Aaron Burr, John Jay, etc.)
 - 2,327 items (items like The Prince)
 - 33M words; vocabulary of 8,000

AARON BURR (Republican)



JOHN JAY (Federalist)

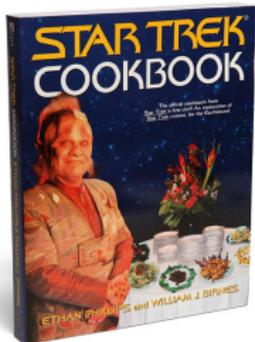




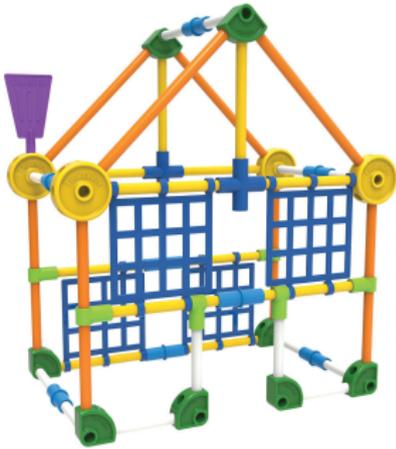
Collaborative topic models

- ▶ Connect text to usage, content to consumption
- ▶ Blend content-based and user-based recommendation
- ▶ Opens new windows into how people read

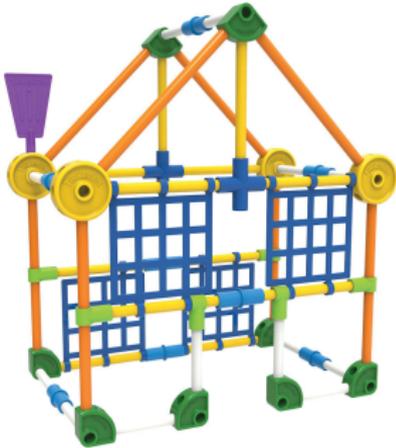
Discussion: Modern Probabilistic Modeling



How to use traditional machine learning and statistics to solve modern problems

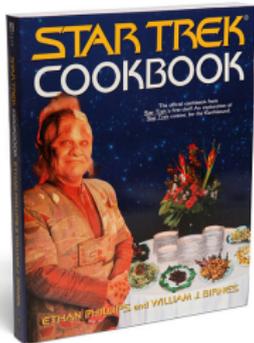


Probabilistic machine learning: tailored models for the problem at hand.

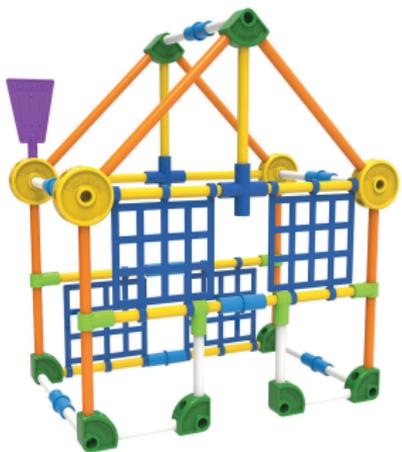


Probabilistic machine learning: tailored models for the problem at hand.

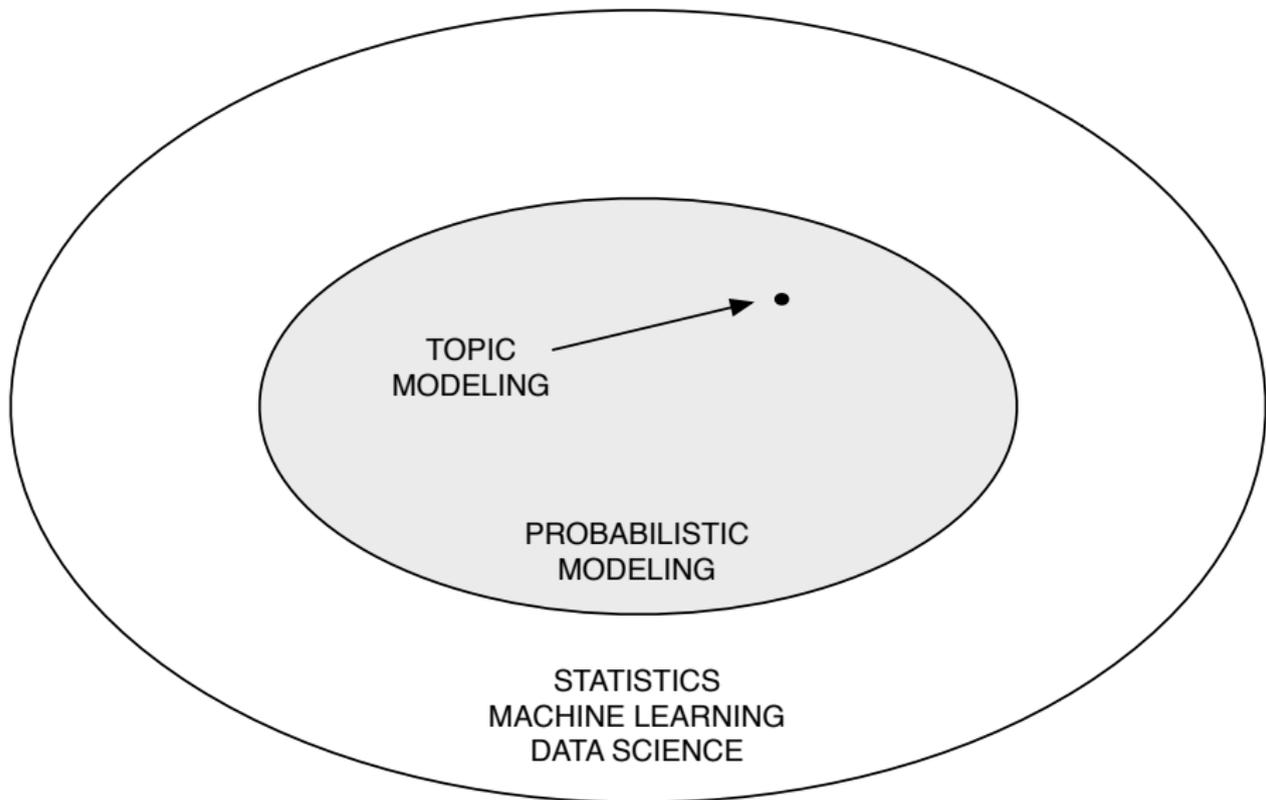
- ▶ Compose and connect reusable parts
- ▶ Driven by disciplinary knowledge and its questions
- ▶ Focus on discovering and using structure in unstructured data
- ▶ Exploratory, observational, causal analyses



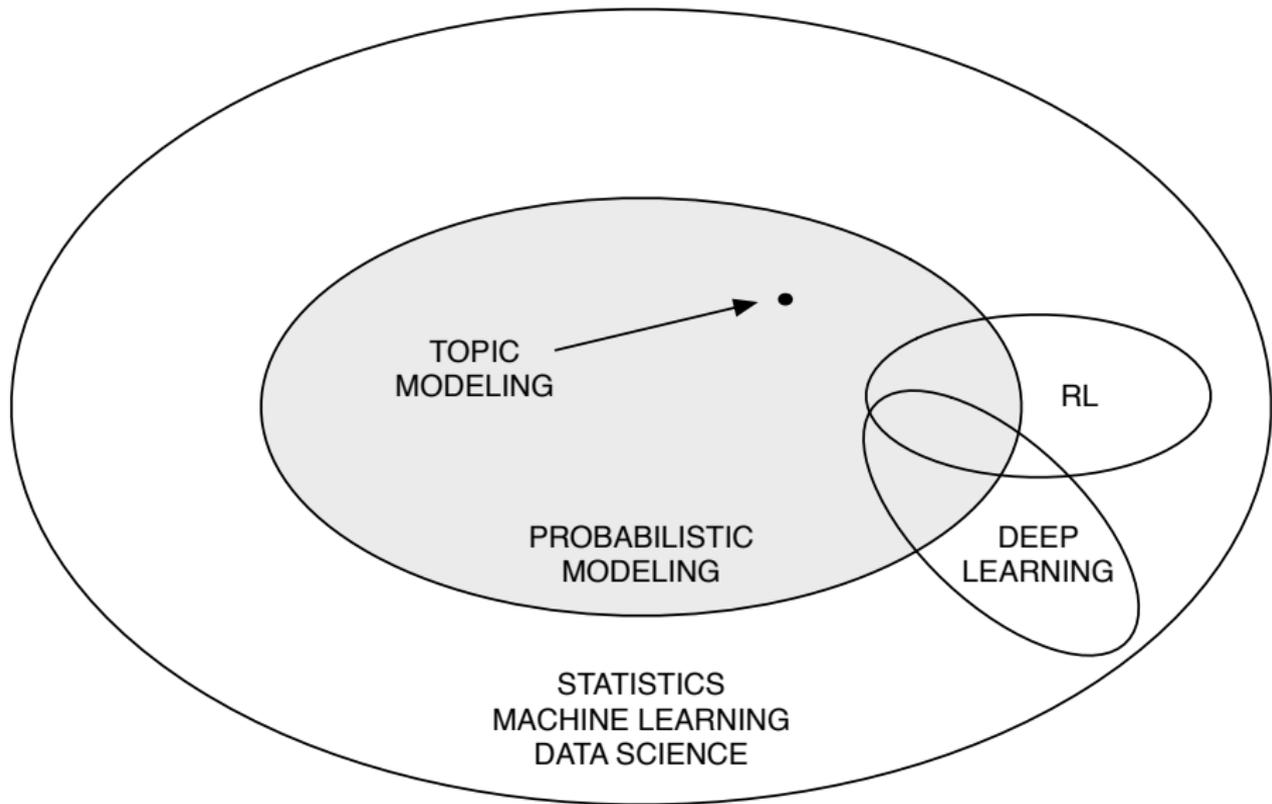
Many software packages available; typically fast and scalable



More challenging to implement; may not be fast or scalable



A big picture

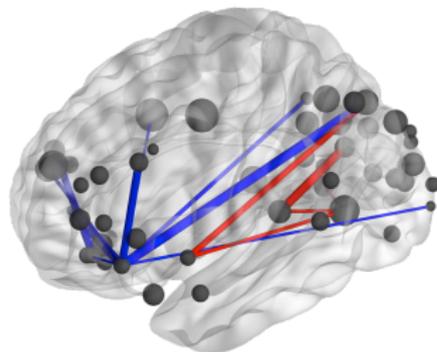
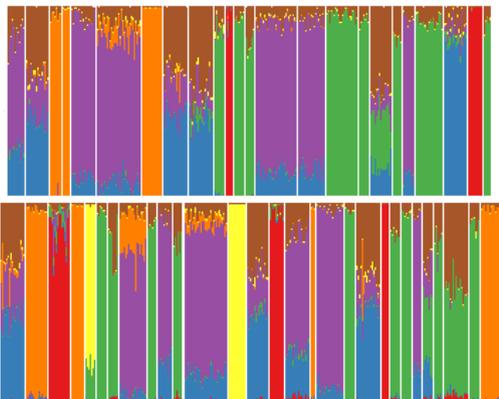
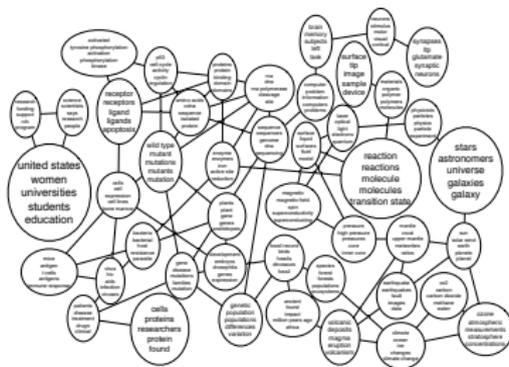
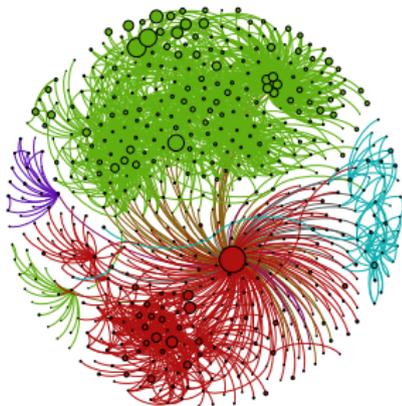


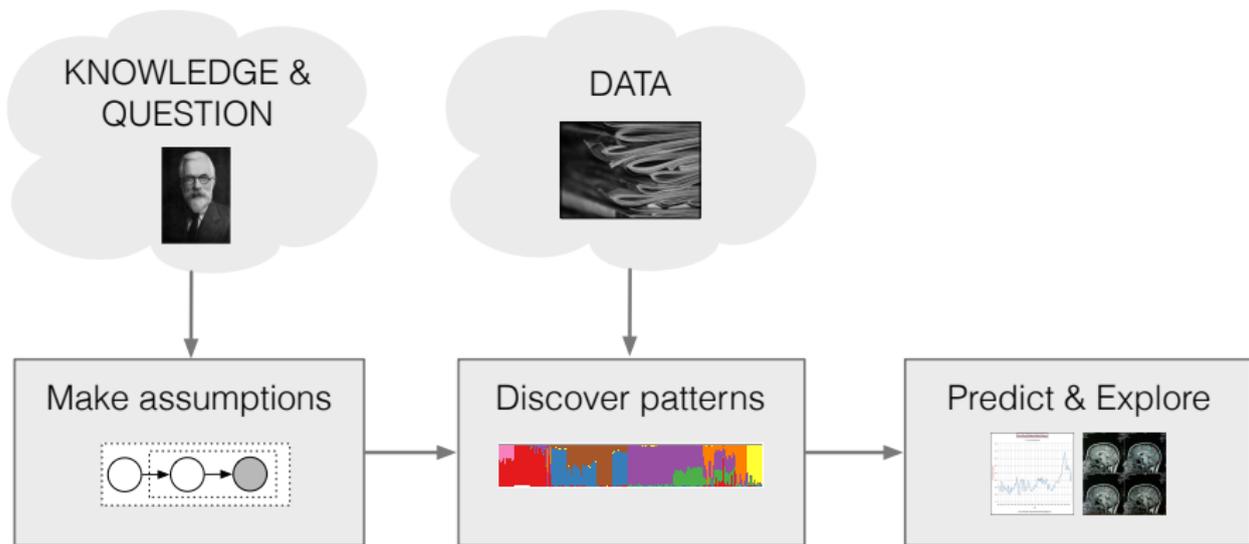
A big picture (not to scale)

II. Discover those patterns from data

$$\nu^* = \arg \max_{\nu} \mathbb{E}_q [\log p(x, z, \beta | \alpha)] + \mathbb{H} [q(z, \beta | \nu)]$$

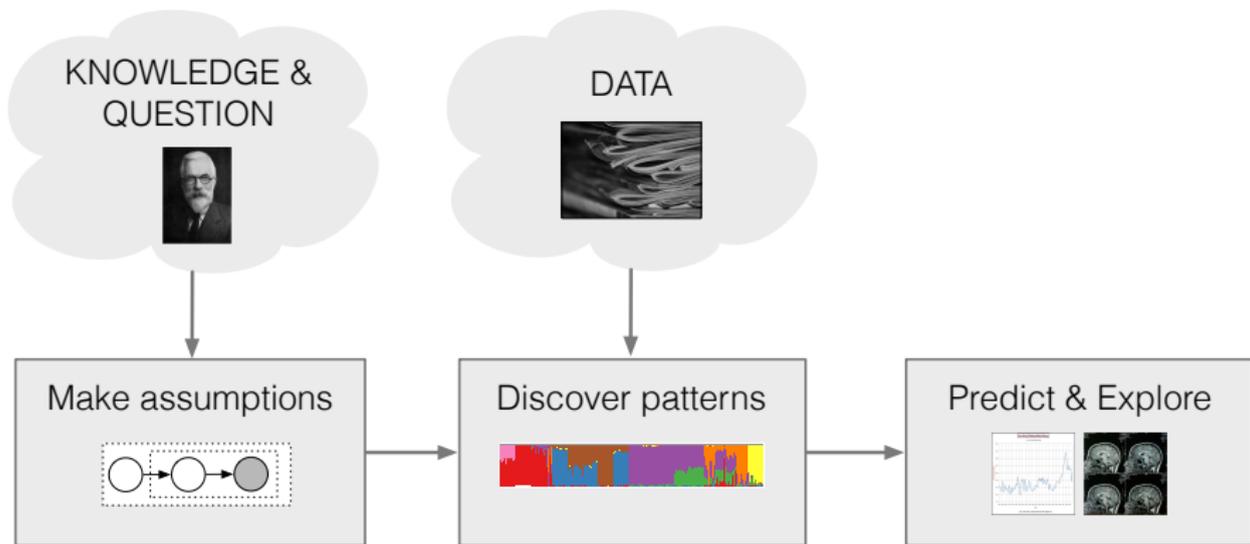
III. Use the discovered patterns to predict about and explore the data





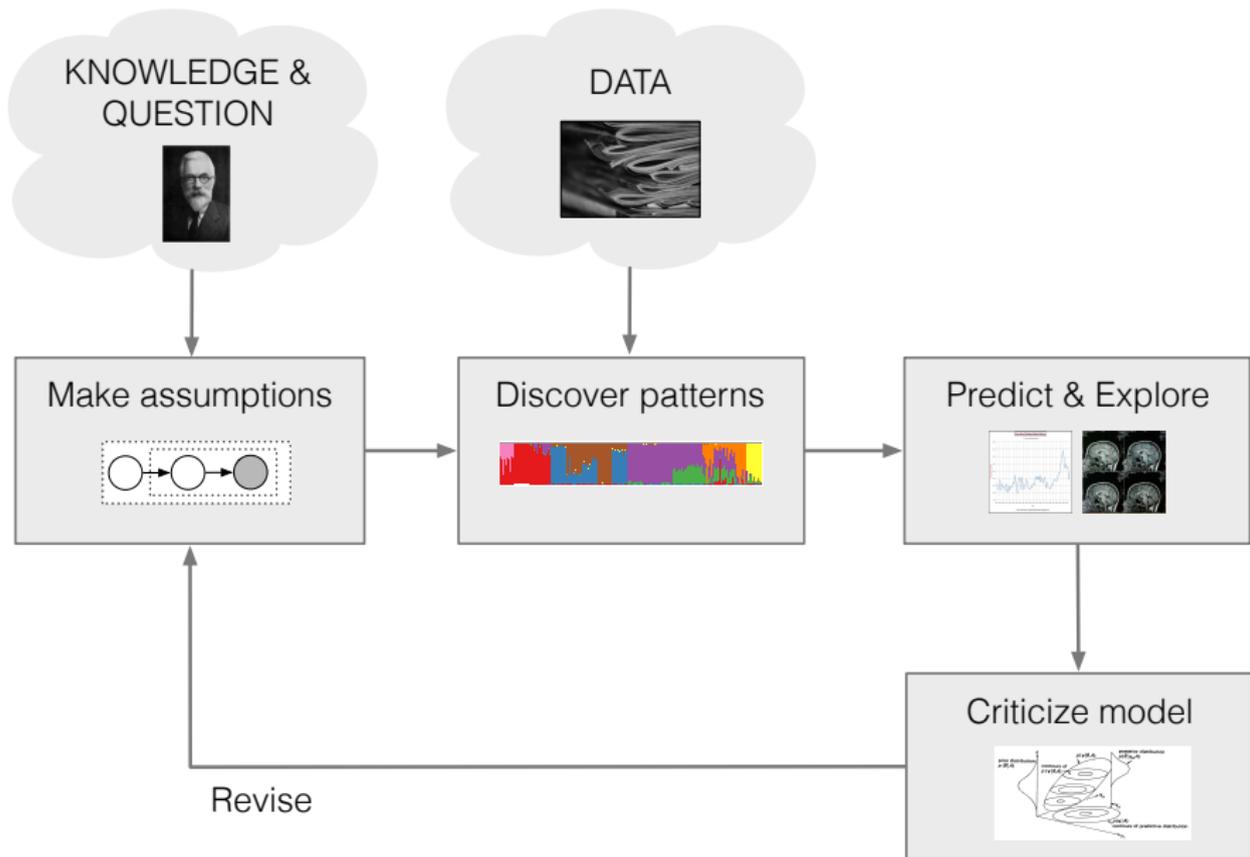
Our perspective:

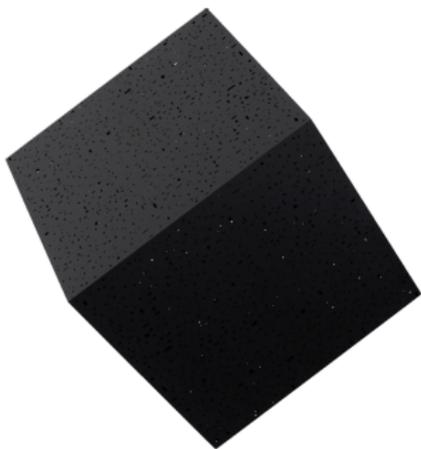
- ▶ Customized data analysis is important to many fields.
- ▶ This pipeline separates assumptions, computation, application.
- ▶ It facilitates solving data science problems.



What we need:

- ▶ **Flexible** and **expressive** components for building models
- ▶ **Scalable** and **generic** inference algorithms
- ▶ **Easy to use** software to stretch probabilistic modeling into new areas

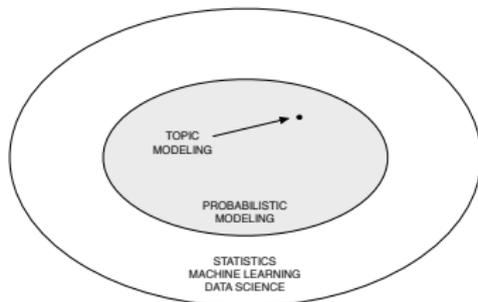
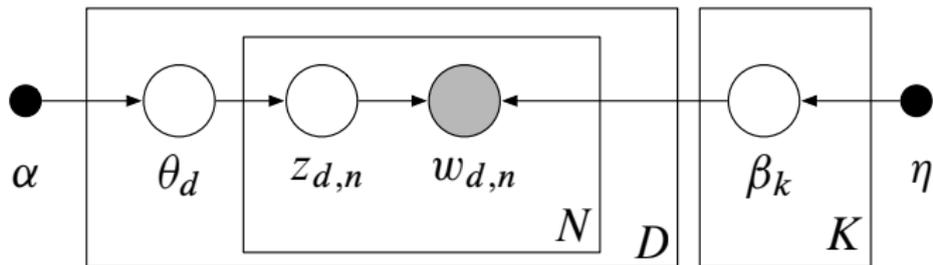




Edward: Probabilistic modeling, inference, and criticism

`github.com/blei-lab/edward`

(lead by Dustin Tran)



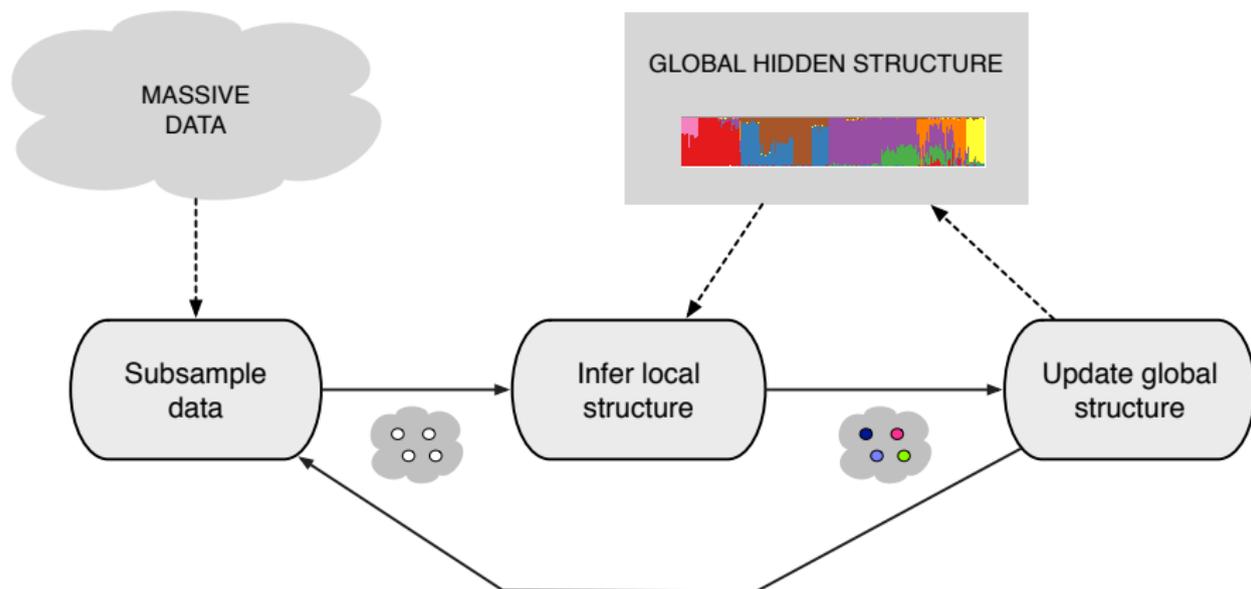


We should seek out unfamiliar summaries of observational material, and establish their useful properties... And still more novelty can come from finding, and evading, still deeper lying constraints.

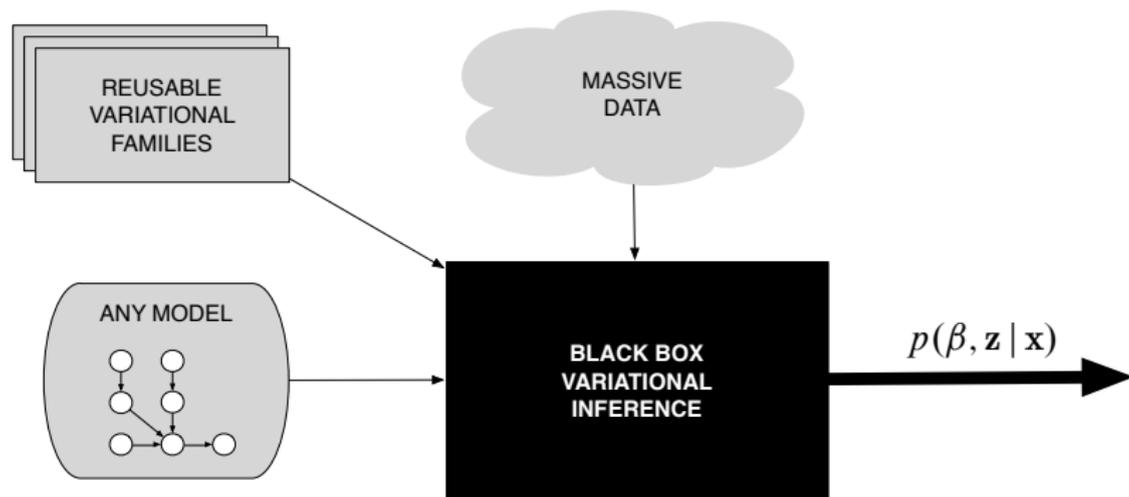
(John Tukey, *The Future of Data Analysis*, 1962)

A few slides about inference

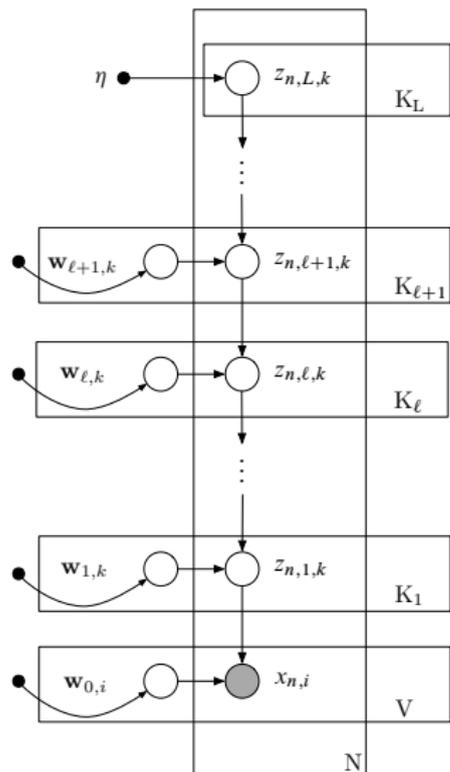
Stochastic variational inference [Hoffman et al., 2013]



Black box variational inference [Ranganath et al., 2014]



- ▶ Easily use variational inference with *any model*
- ▶ No exponential family requirements
- ▶ No mathematical work beyond specifying the model



$$z_{n,L,k} \sim \text{EXP-FAM}(\eta)$$

$$z_{n,\ell,k} \sim \text{EXP-FAM}(g(\mathbf{w}_{\ell,k}^T \mathbf{z}_{n,\ell+1}))$$

$$x_{n,i} \sim \text{EXP-FAM}(g(\mathbf{w}_{0,i}^T \mathbf{z}_{n,1}))$$

Deep Exponential Families

[Ranganath et al., 2015]

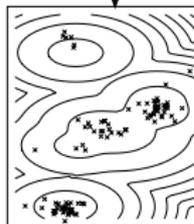
```

data {
  int<lower=1> K;
  int<lower=1> N;
  real y[N];
}

parameters {
  simplex[K] theta;
  real mu[K];
  real<lower=0,upper=10> sigma[K];
}

model {
  real ps[K];
  for (k in 1:K) {
    mu[k] ~ normal(0,10);
  }
  for (n in 1:N) {
    for (k in 1:K) {
      ps[k] <- log(theta[k])
        + normal_log(y[n],mu[k],sigma[k]);
    }
    lp_ <- lp_ + log_sum_exp(ps);
  }
}

```

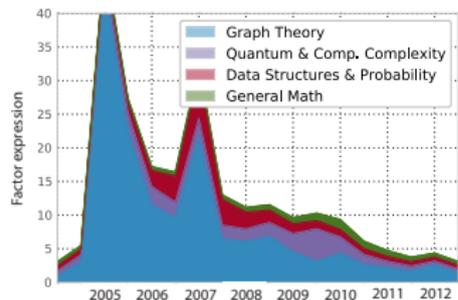
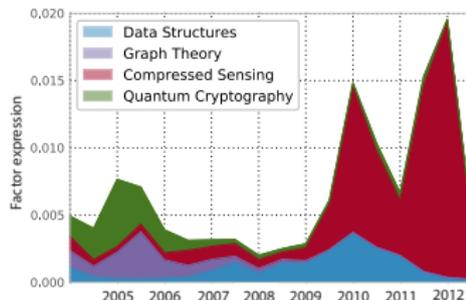
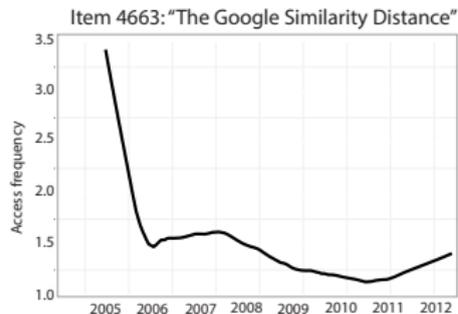
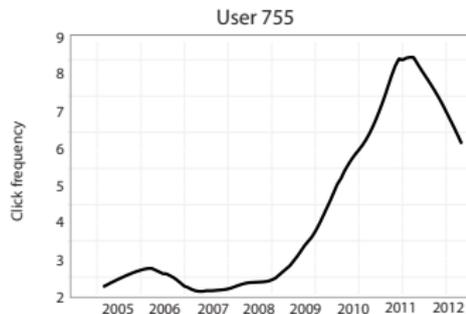


Probabilistic Program

[Kucukelbir et al., 2017]

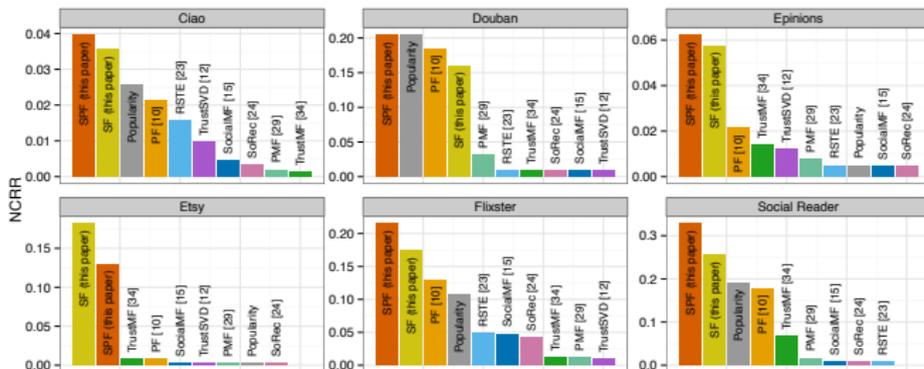
Some recent work about recommendation

Time series recommendation



(with Laurent Charlin, James McInerney, Rajesh Ranganath)

Social recommendation



(with Allison Chaney)